

Mark Scheme (Results)

October 2023

Pearson Edexcel International Advanced Level in Mechanics (WME02) Paper 01

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### **General Marking Guidance**

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

## **General Instructions for Marking**

The total number of marks for the paper is 75.

Edexcel Mathematics mark schemes use the following types of marks:

#### 'M' marks

These are marks given for a correct method or an attempt at a correct method. In Mechanics they are usually awarded for the application of some mechanical principle to produce an equation, e.g. resolving in a particular direction; taking moments about a point; applying a suvat equation; applying the conservation of momentum principle; etc.

The following criteria are usually applied to the equation.

To earn the M mark, the equation

- (i) should have the correct number of terms
- (ii) each term needs to be dimensionally correct

For example, in a moments equation, every term must be a 'force x distance' term or 'mass x distance', if we allow them to cancel 'g' s.

For a resolution, all terms that need to be resolved (multiplied by sin or cos) must be resolved to earn the M mark.

'M' marks are sometimes dependent (DM) on previous M marks having been earned, e.g. when two simultaneous equations have been set up by, for example, resolving in two directions and there is then an M mark for solving the equations to find a particular quantity – this M mark is often dependent on the two previous M marks having been earned.

#### 'A' marks

These are dependent accuracy (or sometimes answer) marks and can only be awarded if the previous M mark has been earned. e.g. M0 A1 is impossible.

### 'B' marks

These are independent accuracy marks where there is no method (e.g. often given for a comment or for a graph).

A and B marks may be f.t. - follow through - marks.

#### General Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes:

- bod means benefit of doubt
- ft means follow through
- the symbol  $\sqrt{}$  will be used for correct ft
- cao means correct answer only
- cso means correct solution only, i.e. there must be no errors in this part of the question to obtain this mark
- isw means ignore subsequent working

- awrt means answers which round to
- SC means special case
- oe means or equivalent (and appropriate)
- dep means dependent
- indep means independent
- dp means decimal places
- sf means significant figures
- \* means the answer is printed on the question paper
- means the second mark is dependent on gaining the first mark

All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.

If a candidate makes more than one attempt at any question:

- If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
- If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.

Ignore wrong working or incorrect statements following a correct answer.

## **General Principles for Mechanics Marking**

(NB specific mark schemes may sometimes override these general principles)

- Rules for M marks:
  - o correct no. of terms;
  - dimensionally correct;
  - all terms that need resolving (i.e. multiplied by cos or sin) are resolved.
- Omission or extra g in a resolution is an accuracy error not method error.
- Omission of mass from a resolution is a method error.
- Omission of a length from a moments equation is a method error.
- Omission of units or incorrect units is not (usually) counted as an accuracy error.
- DM indicates a dependent method mark, i.e. one that can only be awarded if a previous specified method mark has been awarded.
- Any numerical answer which comes from use of g = 9.8 should be given to 2 or 3 SF.
- Use of g = 9.81 should be penalised once per (complete) question.
  - N.B. Over-accuracy or under-accuracy of correct answers should only be penalised *once* per complete question. However, premature approximation should be penalised every time it occurs.
- Marks must be entered in the same order as they appear on the mark scheme.
- In all cases, if the candidate clearly labels their working under a particular part of a question i.e. (a) or (b) or (c)...then that working can only score marks for that part of the question.
- Accept column vectors in all cases.
- Misreads if a misread does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, bearing in mind that after a misread, the subsequent A marks affected are treated as A ft

### **Mechanics Abbreviations**

M(A) Taking moments about A.

N2L Newton's Second Law (Equation of Motion)

NEL Newton's Experimental Law (Newton's Law of Impact)

HL Hooke's Law

SHM Simple harmonic motion

PCLM Principle of conservation of linear momentum

RHS Right hand side

LHS Left hand side

Question	Scheme	Mark	Notes	
1	Accept column vectors throughout this question			
1a	Differentiate <b>r</b> (both components)	M1	In each component at least one power going down by 1	
	$\mathbf{v} = \left(4t^3 - 16t\right)\mathbf{i} + \left(12t - 3\sqrt{t}\right)\mathbf{j}$	A1	Accept as two separate components	
	Equate <b>i</b> component of <b>v</b> to zero and solve for <i>t</i>	DM1	Dependent on the first M1.  Must start with a component of the vector for v  Can have more than one value at this stage.	
	Obtain $(24-3\sqrt{2})\mathbf{j}$ (m s <sup>-1</sup> )	A1	Accept $20\mathbf{j} (\text{m s}^{-1})$ or better. (19.757359) Correct answer only Answer must be a vector	
		[4]		
1b	Differentiate v (both components)	M1	For differentiating their <b>v</b> , even if the method for obtaining it was incorrect. Their <b>v</b> must be a vector.  In each component at least one power going down by 1	
	Obtain $\mathbf{a} = (12t^2 - 16)\mathbf{i} + (12 - \frac{3}{2}t^{-\frac{1}{2}})\mathbf{j}$	A1	Any equivalent form for acceleration	
	Obtain $176i + \frac{45}{4} j (m s^{-2})$	A1	Accept $180\mathbf{i} + 11\mathbf{j} \left( \mathbf{m}  \mathbf{s}^{-2} \right)$ or better ISW	
		[3]		
		(7)		

Question	Scheme				Mark	Notes
2a		PQUY	RSTU	VWXY		
	Mass	$16a^{2}$	$2\times 4a^2$	$2\times 4a^2$	B1	Correct mass ratios (accept
	From	2 <i>a</i>	5 <i>a</i>	а	B1	2:1:1)
	PX					Correct vertical distances
	Moments a	bout <i>PX</i>	or a paral	llel axis	M1	Dimensionally correct
						equation. All terms required
						Allow for an equation within a
						vector equation.
	$16a^2 \times 2a +$	$8a^2 \times 5a$	$+8a^2 \times a$	$=32a^2d$		Correct unsimplified equation
	(=(16+	$(0,0)$ $a^2$	1)		A1	Allow for an equation within a
			,			vector equation.
	or equivale			is		Could have y for d here o.e.
	80a = 32d	$\Rightarrow d = \frac{5}{3}$	a *		A1*	Obtain given answer from
		2				correct working. At least one stage of simplifying the
						moments equation is required.
						e.g. $32a^3 + 40a^3 + 8a^3$ seen,
						or they might have simplified
						the mass ratios at the start.
						Must get to $d = \dots$ in the final
					r = 1	line
2b	Moments of	hout PO	or a para	llal avic	[5] M1	Dimensionally correct
20	Moments about $PQ$ or a parallel axis			iici axis	IVII	equation.
						All terms required
	$16a^2 \times 2a +$	$8a^2 \times 3a$	$+8a^2 \times 5a$	$\overline{a}$	A1ft	Unsimplified equation with at
	_(16±8	$+8)a^2 \times$	h			most one error. Follow their
	`	/		.•	A1	mass ratios.
	or equivalent for a parallel axis $\Rightarrow h = 3a \text{ from } PQ$ The working for the first 4 marks my			A1	Correct unsimplified equation a from YT, 3a from XW	
				ust be seen or used in part (b)		
	Correct use				M1	With their 3a e.g.
	of a relevan	_	- 1111G UIV			
		-				$\tan \theta = \frac{3}{4 - \frac{5}{2}}$
	$\tan \theta = 2$				A1	Correct only
	11110 - 2				[6]	contect only
2c	Complete r	nethod to	obtain a	n	M1	e.g. Moments about Q
	equation in					Dimensionally correct
						equation.
	$3a \times Mg = 4$	$4a \times F$			A1	Correct unsimplified equation
						Condone if <i>a</i> missing
	2				A 1	throughout Correct only
	$F = \frac{3}{4}$	Mg			A1	Correct only
	4				[3]	
					(14)	
	1				(17)	<u> </u>

Question	Scheme	Mark	Notes
3	Form impulse-momentum equation	M1	Dimensionally correct.
			Accept answers in "vector" form, or as
			separate components. Condone sine /
			cosine confusion.
	One correct equation	A1	e.g. one correct component of
			$ \left  \begin{pmatrix} I\cos 60^{\circ} \\ I\sin 60^{\circ} \end{pmatrix} \right  = \frac{1}{4} \left[ \begin{pmatrix} 12\cos \alpha \\ 12\sin \alpha \end{pmatrix} - \begin{pmatrix} 8 \\ 0 \end{pmatrix} \right] $
			$\left[ \left( I \sin 60^{\circ} \right)^{-} \overline{4} \left[ \left( 12 \sin \alpha \right)^{-} \left( 0 \right) \right] \right]$
			$ \left( = \begin{pmatrix} 3\cos\alpha - 2 \\ 3\sin\alpha \end{pmatrix} \right) $
			$\left(\begin{array}{ccc} 3\sin\alpha \end{array}\right)$
			$ \left  \begin{pmatrix} I\cos 60^{\circ} \\ I\sin 60^{\circ} \end{pmatrix} \right  = \frac{1}{4} \left  \begin{pmatrix} v_x \\ v_y \end{pmatrix} - \begin{pmatrix} 8 \\ 0 \end{pmatrix} \right  $
			$\left  \left( I \sin 60^{\circ} \right)^{=} \frac{1}{4} \left[ \left( v_{y} \right)^{-} \left( 0 \right) \right] \right $
			$ = \begin{pmatrix} 3\cos\alpha - 2 \\ 3\sin\alpha \end{pmatrix} $
			( ( 5 5 11 6 7 ))
			if working parallel and perpendicular to the initial direction
			or one of $8\sin 60^\circ = 12\cos(30^\circ + \alpha)$
			or $I = 0.25(12\sin(30^{\circ} + \alpha) - 8\cos 60^{\circ})$
			if working parallel and perpendicular to the impulse
	Form a second impulse-momentum equation	M1	
	correct second equation	A1	
	Complete method to solve for <i>I</i>	DM1	Dependent on the two preceding M marks. e.g. from
			$36 = (I+4)^2 + 3I^2  (4I^2 + 8I - 20 = 0)$
	$I = \sqrt{6} - 1$ (or 1.45 or 1.4)	A1	
		[6]	
3 alt	2	M1	Use of $I = mv - mu$ to draw a vector triangle. Dimensionally consistent.
	120° I	A1	Correct diagram
	Form an equation in <i>I</i>	M1	e.g. by using cosine rule
	$4 + I^2 - 4I\cos 120^\circ = 9$	A1	Correct unsimplified equation
			A correct cosine rule equation can imply the first M1A1 if no diagram
l I			seen
			Donardant on the 2 preceding M marks
	Solve for <i>I</i>	DM1	Dependent on the 2 preceding M marks $I^2 + 2I - 5 = 0$
	Solve for <i>I</i> $I = \sqrt{6} - 1 \text{ (or 1.45 or 1.4)}$	DM1 A1	Dependent on the 2 preceding W marks $I^2 + 2I - 5 = 0$

Question	Scheme	Mark	Notes			
4a	$4 - gT_1 = 0$ or $T_1 = \frac{\sqrt{32}\sin 45^\circ}{g}$	M1	Complete method using <i>suvat</i>			
	$T_1 = 0.408 (0.41)$	A1	3 sf or 2 sf only. Not $\frac{20}{49}$			
		[2]				
4b	Height of <i>Q</i> above <i>P</i> :	M1	Complete method using <i>suvat</i> and 7 and 4 for the initial vertical components			
	$h = \left(7T_1 - \frac{1}{2}gT_1^2\right) - \left(4T_1 - \frac{1}{2}gT_1^2\right)  (=3T_1)$	A1	Correct unsimplified expression in $T_1$ or their $T_1$ They do not need to have substituted for $T_1$ (2.0408 0.8163)			
	h = 1.2  (m)	A1ft	2 sf only $(3 \times their T_1)$			
		[3]				
4c	Correct time for <i>P</i> to reach <i>B</i> . ( $\frac{40}{49}$ , 0.816, or $\frac{8}{g}$ or better)	B1	Seen or implied.			
	Vertical component of speed $= 7 - g \times 2T_1  (=-1)$	M1	Complete method using <i>suvat</i> with $2T_1$ or their $t$ for the time at $B$ M0 if not using 7			
	$\tan \alpha = \pm \frac{their  1}{5}$	M1	Correct use of <i>their</i> 1 and 5 to find an equation in a relevant angle (e.g. $90 - \alpha$ )			
	$\alpha = 11$	A1	11 or better (e.g. 11.3)			
	If they use $T_1$ in place of $2T_1$ can score B0M0M1A0					
		[4]				
4d	Form an equation in $T_2$ only	M1	Complete method using <i>suvat</i> and perpendicular gradients.  e.g. $\binom{5}{7}$ . $\binom{5}{7-gT_2} = 0$			
			Condone sign errors			
			(Vertical component of speed $=\pm\frac{25}{7}$ )			
			(perpendicular direction is downwards at 35.5° to the horizontal)			
	$-\frac{25}{7} = 7 - gT_2$	A1	Correct unsimplified equation			
	$T_2 = 1.08 \text{ or } T_2 = 1.1$	A1	3 sf or 2 sf only			
		[3]				
		(12)				

Question	Scheme	Mark	Notes
5a	Use of $P = Fv \left( F = \frac{500}{6} \right)$	M1	
	Equation of motion	M1	Dimensionally correct.
			Required terms and no extras
	F - 60 = 80a	A1	Correct unsimplified equation in <i>F</i>
	$a = \frac{7}{24} \left( \text{m s}^{-2} \right)$	A1	0.29 or better (0.291666666)
		[4]	
5b	Gain in KE = $\frac{1}{2} \times 80 \times 8^2$ (J) (= 2560(J))		
	Gain in GPE =	B1	Any one correct (seen or
	$80 \times 9.8 \times 300 \text{ (J)} (= 235200 \text{ (J)})$	B1	implied)
	Work done against resistance = 20000×60		A second term correct (seen or implied)
	2000000		(KE gain + GPE gain = 237760 J)
	Use of <i>suvat</i> and $F = ma$ is M0A0A0		
	expression for combined work and energy	M1	All terms required and no double counting. Mass replaced with 80. Condone sign errors. Dimensionally correct. Condone error in zeros in 20000
	Total work done = $40 \times 64 + 80 \times 9.8 \times 300 + 20000 \times 60$	A1	Correct unsimplified expression for the work done
	1440(kJ)or 1400(kJ)	A1	Accept answers in joules. 3 sf or 2 sf (1437760)
		[5]	, ,
5c	Equation of motion	M1	Dimensionally correct.
			Required terms and no extras
	$F - 60 - 80g \times \sin \alpha = 0$	A1	Unsimplified equation in <i>P</i> or
	$\frac{P}{7} - 60 - 80g \times \frac{1}{20} = 0$	A 1	F with at most one error
		A1	Correct unsimplified equation in <i>P</i>
	P = 694  or  P = 690	A1	3sf or 2 sf only
		[4]	222 31 2 31 3111
		(13)	
	<u>l</u>	()	L

Question	Scheme	Mark	Notes
ба	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		
	W $H$ $A$	M1	Need all terms and no extras.
		1411	Dimensionally consistent. Condone sign
	M0 if there is no resolving $4a\cos 30^{\circ} \times W + 8a\cos 30^{\circ} \times \frac{W}{4}$	A1	errors and sine/cosine confusion.  Correct unsimplified equation
	$= 5a\cos 30^{\circ} \times T$ $6W = 5T \Rightarrow T = \frac{6}{5}W  *$	A1*	Obtain <b>given answer</b> from correct working, e.g. show cancelling of the common factors or some simplification of the moments equation
		[3]	the moments equation
6b	They need 2 equations. Award M1A1 second correct equation. Common alt $M(B)$ : $T \cos 30^{\circ} \times 3a + V \cos 30^{\circ} \times 8a = M(C)$ : $W \cos 30^{\circ} \times a + H \cos 60^{\circ} \times 5a = $ Perpendicular to $\cot \frac{1}{4}W \cos 30^{\circ} + W \cot 30^{\circ}$ Parallel to $\cot \frac{1}{4}W \cos 60^{\circ} + T \cos 60^{\circ}$	ternatives: $W \cos 30^{\circ} > \frac{1}{4}W \cos 30^{\circ} + H$ $\cos 30^{\circ} + H$	$^{\circ} \times 3a + V \cos 30^{\circ} \times 5a$ $\cos 60^{\circ} = T \cos 30^{\circ} + V \cos 30^{\circ}$
	First equation dimensionally correct. Condone sine/cosine confusion and sign errors	M1	e.g. Resolve horizontally
	Correct unsimplified equation	A1	$H = T\cos 30^{\circ}  \left(H = \frac{3\sqrt{3}}{5}W\right)$
	Second equation dimensionally correct. Condone sine/cosine confusion and sign errors	M1	e.g. resolve vertically
	Correct unsimplified equation	A1	$V + T\cos 60^{\circ} = W + \frac{W}{4}  \left(V = \frac{13}{20}W\right)$
	$ R  = \sqrt{V^2 + H^2} \text{ or }  R ^2 = V^2 + H^2$	DM1	Correct use of Pythagoras Dependent on two preceding M marks.
	$ R  = \frac{W}{20}\sqrt{3\times144 + 169} = \frac{\sqrt{601}}{20}W$	A1	1.2W or better (1.22576)
		[6] (9)	

Question	Scheme	Mark	Notes
7a	2u		
	$\longrightarrow$ $\stackrel{3u}{\longleftarrow}$		
	$\left( \begin{array}{c} P \\ 4m \end{array} \right) \left( \begin{array}{c} Q \\ 2m \end{array} \right)$		
	$\langle x \rangle$		
	Equation for CLM	M1	Dimensionally correct.
	Equation for CEIVI	IVII	All terms required.
			Condone sign errors.
	8mu - 6mu = 2my - 4mx	A1	Correct unsimplified equation
	(u = y - 2x)		
	Equation for kinetic energy	M1	Dimensionally correct. Correct masses paired
	$\left(\frac{1}{2} \text{ or } 2 \text{ must be used}\right)$	IVII	with correct velocities. All terms required. No
	$(\frac{1}{2})$ of 2 must be used)		sign errors. Condone 2 on the wrong side.
	$2mx^{2} + my^{2} = \frac{1}{2} \left( 2m \times 4u^{2} + m \times 9u^{2} \right)$	A1	Correct unsimplified equation
	$(17u^2 = 4x^2 + 2y^2)$		
	Solve for $y$ :	DM1	Some working must be shown to obtain the
	$17u^2 = 2y^2 + (y - u)^2$	Divil	quadratic in $y$ (and $u$ ).
	` '		Dependent on the preceding M marks
	$\Rightarrow 3y^2 - 2yu - 16u^2 = 0$		$\left( (3y - 8u)(y + 2u) = 0 \right)$
	$\Rightarrow y = \frac{8}{3}u$ *	A1*	Obtain given answer from correct working
		[6]	
7b	Use of Impact Law: $x + y = e \times 5u$	M1	Condone sign errors but must be used the right
	1(0) 0		way round.
	$\left  \frac{1}{2} \left( \frac{\delta}{2} u - u \right) + \frac{\delta}{2} u \right $	A 1	Correct unsimplified equation. $\left(x = \frac{5u}{6}\right)$
	$e = \frac{\frac{1}{2} \left(\frac{8}{3}u - u\right) + \frac{8}{3}u}{5u}$	A1	( 6)
	5 <i>u</i>	A 1	G 1
	$=\frac{7}{}$	A1	Correct only
	10		
7.	0	[3]	A11 I
7c	Velocity of Q after impact = $f \times \frac{8}{3}u$	B1	Allow ±
	3		
	No collision if $f \times \frac{8}{3}u \le \frac{5}{6}u$	M1	Correct inequality with their values
	i.e. speed of $P \ge$ speed of $Q$		Accept strict inequality. Dimensionally correct.
	$\Rightarrow 0 < f \le \frac{5}{16}$	A1	Both ends required. $(0 < f \le 0.3125)$
		[3]	, , ,
7d	x	M1	Subtraction seen or implied with <i>their</i> $\frac{1}{4}$ <i>y</i>
	Use of $I = \pm 2m \left( y - \left( -\frac{1}{4} y \right) \right)$		Requires correct mass
			Requires correct impact law
	$ I  = \frac{20}{3}mu$	A1	Or equivalent. Must be positive
	$ I  = \frac{1}{3}mu$		6.7mu or better
			Condone $-\frac{20}{3}mu \rightarrow \frac{20}{3}mu$ with no
			3 3
			explanation
		[2]	
		(14)	